

6.7

1) $(k - 7)(k + 2) = 0$
 $k - 7 = 0 \quad k + 2 = 0$
 $\underline{+7 \quad +7} \quad \underline{-2 \quad -2}$
 $k = 7 \quad k = -2$

3) $(x - 1)(x + 4) = 0$
 $x - 1 = 0 \quad x + 4 = 0$
 $\underline{+1 \quad +1} \quad \underline{-4 \quad -4}$
 $x = 1 \quad x = -4$

5) $6x^2 - 150 = 0$
 $6(x^2 - 25) = 0$
 $6(x + 5)(x - 5) = 0$
 $x + 5 = 0 \quad x - 5 = 0$
 $\underline{-5 \quad -5} \quad \underline{+5 \quad +5}$
 $x = -5 \quad x = 5$

7) $2n^2 + 10n - 28 = 0$
 $2(n^2 + 5n - 14) = 0$
 $2(n + 7)(n - 2) = 0$
 $n + 7 = 0 \quad n - 2 = 0$
 $\underline{-7 \quad -7} \quad \underline{+2 \quad +2}$
 $n = -7 \quad n = 2$

9) $7x^2 + 26x + 15 = 0$
 $7x^2 + 5x + 21x + 15 = 0$
 $x(7x + 5) + 3(7x + 5) = 0$
 $(7x + 5)(x + 3) = 0$
 $7x + 5 = 0 \quad x + 3 = 0$
 $\underline{-5 \quad -5} \quad \underline{-3 \quad -3}$
 $\frac{7x}{7} = \frac{-5}{7} \quad x = -3$
 $x = -\frac{5}{7}$

11) $5n^2 - 9n - 2 = 0$
 $5n^2 - 10n + n - 2 = 0$
 $5n(n - 2) + 1(n - 2) = 0$
 $(n - 2)(5n + 1) = 0$
 $n - 2 = 0 \quad 5n + 1 = 0$
 $\underline{+2 \quad +2} \quad \underline{-1 \quad -1}$
 $n = 2 \quad \frac{5n}{5} = \frac{-1}{5}$
 $n = -\frac{1}{5}$

13) $x^2 - 4x - 8 = -8$
 $x^2 - 4x = 0$
 $x(x - 4) = 0$
 $x = 0 \quad x - 4 = 0$
 $\underline{+4 \quad +4}$
 $x = 4$

15) $x^2 - 4x - 1 = -5$
 $x^2 - 4x + 4 = 0$
 $(x - 4)(x - 1) = 0$
 $x - 4 = 0 \quad x - 1 = 0$
 $\underline{+4 \quad +4} \quad \underline{+1 \quad +1}$
 $x = 4 \quad x = 1$

17) $49p^2 + 371p - 241 = 0$
 $7(7p^2 + 53p - 24) = 0$
 $7(7p^2 - 3p + 56p - 24) = 0$
 $7(p(7p - 3) + 8(7p - 3)) = 0$
 $7(7p - 3)(p + 8) = 0$
 $7p - 3 = 0 \quad p + 8 = 0$
 $\underline{+3 \quad +3} \quad \underline{-8 \quad -8}$
 $\frac{7p}{7} = \frac{3}{7} \quad p = -8$
 $p = \frac{3}{7}$

19) $7x^2 + 17x - 20 = -8$

$$\begin{array}{r} +8 \quad +8 \\ \hline 7x^2 + 17x - 12 = 0 \end{array}$$

$$\begin{array}{r} -84 \\ -4 \quad 21 \\ \hline 17 \end{array}$$

$$7x^2 - 4x + 21x - 12 = 0$$

$$x(7x - 4) + 3(7x - 4) = 0$$

$$(7x - 4)(x + 3) = 0$$

$$7x - 4 = 0 \quad x + 3 = 0$$

$$\begin{array}{r} +4 \quad +4 \\ \hline 7x = \frac{4}{7} \end{array}$$

$$x = \frac{4}{7}$$

21) $7r^2 + 84 = -49r$

$$\begin{array}{r} +49r \quad +49r \\ \hline 7r^2 + 49r + 84 = 0 \end{array}$$

$$\begin{array}{r} 12 \\ 4 \quad 3 \\ \hline 7 \end{array}$$

$$7(r^2 + 7r + 12) = 0$$

$$7(r^2 + 7r + 12) = 0$$

$$7(r + 4)(r + 3) = 0$$

$$r + 4 = 0 \quad r + 3 = 0$$

$$\begin{array}{r} -4 \quad -4 \\ \hline r = -4 \quad r = -3 \end{array}$$

23) $x^2 - 6x = 16$

$$\begin{array}{r} -16 \quad -16 \\ \hline x^2 - 6x - 16 = 0 \end{array}$$

$$\begin{array}{r} -16 \\ -8 \quad 2 \\ \hline -6 \end{array}$$

$$(x - 8)(x + 2) = 0$$

$$x - 8 = 0 \quad x + 2 = 0$$

$$\begin{array}{r} +8 \quad +8 \\ \hline x = 8 \quad x = -2 \end{array}$$

25) $3v^2 + 7v = 40$

$$\begin{array}{r} -40 \quad -40 \\ \hline 3v^2 + 7v - 40 = 0 \end{array}$$

$$\begin{array}{r} -120 \\ 15 \quad -8 \\ \hline 7 \end{array}$$

$$3v^2 + 15v - 8v - 40 = 0$$

$$3v(v + 5) - 8(v + 5) = 0$$

$$(v + 5)(3v - 8) = 0$$

$$v + 5 = 0 \quad 3v - 8 = 0$$

$$\begin{array}{r} -5 \quad -5 \\ \hline v = -5 \quad \frac{3v}{3} = \frac{8}{3} \end{array}$$

$$v = \frac{8}{3}$$

27) $35x^2 + 120x = -45$

$$\begin{array}{r} +45 \quad +45 \\ \hline 35x^2 + 120x + 45 = 0 \end{array}$$

$$\begin{array}{r} 63 \\ 3 \quad 21 \\ \hline 24 \end{array}$$

$$5(7x^2 + 24x + 9) = 0$$

$$5(7x^2 + 3x + 21x + 9) = 0$$

$$5(x(7x + 3) + 3(7x + 3)) = 0$$

$$5(7x + 3)(x + 3) = 0$$

$$7x + 3 = 0 \quad x + 3 = 0$$

$$\begin{array}{r} -3 \quad -3 \\ \hline \frac{7x}{7} = \frac{-3}{7} \end{array}$$

$$x = -\frac{3}{7}$$

29) $4k^2 + 18k - 23 = 6k - 7$

$$\begin{array}{r} -6k + 7 \quad -6k + 7 \\ \hline 4k^2 + 12k - 16 = 0 \end{array}$$

$$\begin{array}{r} 4 \\ 4 \quad -1 \\ \hline 3 \end{array}$$

$$4(k^2 + 3k - 4) = 0$$

$$4(k + 4)(k - 1) = 0$$

$$k + 4 = 0 \quad k - 1 = 0$$

$$\begin{array}{r} -4 \quad -4 \quad +1 \quad +1 \\ \hline k = -4 \quad k = 1 \end{array}$$

31) $9x^2 - 46 + 7x = 7x + 8x^2 + 3$

$$\begin{array}{r} -8x^2 - 3 \quad -7x - 7x - 8x^2 - 3 \\ \hline x^2 - 49 = 0 \end{array}$$

$$(x + 7)(x - 7) = 0$$

$$x + 7 = 0 \quad x - 7 = 0$$

$$\begin{array}{r} -7 \quad -7 \quad +7 \quad +7 \\ \hline x = -7 \quad x = 7 \end{array}$$

33) $2m^2 + 19m + 40 = -2m$

$$\begin{array}{r} +2m \quad +2m \\ \hline 2m^2 + 21m + 40 = 0 \end{array}$$

$$\begin{array}{r} 80 \\ 5 \quad 16 \\ \hline 21 \end{array}$$

$$2m^2 + 4m + 16m + 40 = 0$$

$$m(2m + 5 + 8(2m + 5)) = 0$$

$$(2m + 5)(m + 8) = 0$$

$$2m + 5 = 0 \quad m + 8 = 0$$

$$\begin{array}{r} -5 \quad -5 \quad -8 \quad -8 \\ \hline \frac{2m}{2} = \frac{-5}{2} \quad m = -8 \end{array}$$

$$m = -\frac{5}{2}$$

$$\begin{aligned}
 35) \quad & 40p^2 + 183p - 168 = p + 5p^2 \\
 & \underline{-5p^2} \quad \underline{-p} \quad \underline{-p - 5p^2} \\
 & 35p^2 + 182p - 168 = 0 \quad \cancel{-120} \\
 & 7(5p^2 + 26p - 24) = 0 \quad \cancel{-4} \quad \cancel{30} \\
 & 7(5p^2 - 4p + 30p - 24) = 0 \\
 & 7(p(5p - 4) + 6(5p - 4)) = 0 \\
 & 7(5p - 4)(p + 6) = 0 \\
 & 5p - 4 = 0 \quad p + 6 = 0 \\
 & \underline{\quad +4 \quad +4 \quad -6 \quad -6} \\
 & \frac{5p}{5} = \frac{4}{5} \quad p = -6 \\
 & p = \frac{4}{5}
 \end{aligned}$$