

9.9

$$1) \frac{xy}{y} = \frac{72}{y} \quad x = \frac{72}{y}$$

$$\frac{(x+2)(y-4)}{y-4} = \frac{128}{y-4}$$

$$x + 2 = \frac{128}{y-4}$$

$$y(y-4) \frac{72}{y} + 2y(y-4) = \frac{128}{y-4} y(y-4)$$

LCD:  $y(y-4)$

$$72(y-4) + 2y(y-4) = 128y$$

$$72y - 288 + 2y^2 - 8y = 128y$$

$$2y^2 + 64y - 288 = 128y$$

$$\begin{array}{r} -128y \\ -128y \\ \hline 2y^2 - 64y - 288 = 0 \end{array}$$

$$y^2 - 32y - 144 = 0$$

$$\begin{array}{r} +144 +144 \\ \hline y^2 - 32y = 144 \end{array}$$

$$(32 \cdot \frac{1}{2})^2 = 16^2 = 256$$

$$y^2 - 32y + 256 = 144 + 256$$

$$\sqrt{(y-16)^2} = \sqrt{400}$$

$$y - 16 = \pm 20$$

$$\begin{array}{r} +16 +16 \\ \hline y = 36, -4 \end{array}$$

$$x = \frac{72}{36} = 2 \quad x = \frac{72}{-4} = -18$$

$$(2, 36), (48, -4)$$

$$3) \frac{xy}{y} = \frac{150}{y} \quad x = \frac{150}{y}$$

$$\frac{(x-6)(y+1)}{y+1} = \frac{64}{y+1}$$

$$x - 6 = \frac{64}{y+1}$$

$$\frac{150y}{y} (y(y+1)) - 6(y(y+1)) = \frac{64}{y+1} (y(y+1))$$

LCD:  $(y(y+1))$

$$150(y+1) - 6y(y+1) = 64y$$

$$150y + 150 - 6y^2 + 6y = 64y$$

$$-6y^2 + 156y + 150 = 64y$$

$$+6y^2 - 156y - 150 \quad +6y^2 - 156y - 150$$

$$\begin{array}{r} 0 \\ 0 = \frac{6y^2}{2} - \frac{80y}{2} - \frac{150}{2} \\ 0 = 3y^2 - 40y - 75 \\ 0 = (3y+5)(y-15) \end{array}$$

$$3y + 5 = 0 \quad y - 15 = 0$$

$$\begin{array}{r} -5 -5 +15 +15 \\ \hline \frac{3y}{3} = -\frac{5}{3} \quad y = 15 \end{array}$$

$$y = -\frac{5}{3} \quad x = \frac{150}{15} = 10$$

$$x = \frac{150}{-\frac{5}{3}} = 150 \left(-\frac{3}{5}\right) = -90$$

$$\left(-90, -\frac{5}{3}\right), (10, 15)$$

5)  $\frac{xy}{y} = \frac{45}{y} \quad x = \frac{45}{y}$   
 $\frac{(x+2)(y+1)}{y+1} = \frac{70}{y+1}$   
 $x + 2 = \frac{70}{y+1}$   
 $\frac{45}{y} (y(y+1)) + 2(y(y+1)) = \frac{70}{y+1} (y(y+1))$   
*LCD: (y(y+1))*  
 $45(y+1) + 2y(y+1) = 70y$   
 $45y + 45 + 2y^2 + 2y = 70y$   
 $2y^2 + 47y + 2y = 70y$   
 $\begin{array}{r} -70y \\ \hline 2y^2 - 23y + 45 = 0 \end{array}$   
 $(2y - 5)(y - 9) = 0$   
 $2y - 5 = 0 \quad y - 9 = 0$   
 $\begin{array}{r} +5 \quad +5 \\ \hline 2y = 5 \end{array} \quad \begin{array}{r} +9 \quad +9 \\ \hline y = 9 \end{array}$   
 $y = \frac{5}{2} \quad x = \frac{45}{9} = 5$   
 $x = \frac{45}{\frac{5}{2}} = 45 \cdot \frac{2}{5} = 18$

$$\left(18, \frac{5}{2}\right), (5, 9)$$

7)  $\frac{xy}{y} = \frac{90}{y} \quad x = \frac{90}{y}$   
 $\frac{(x-5)(y+1)}{y+1} = \frac{120}{y+1}$   
 $x - 5 = \frac{120}{y+1}$   
 $\frac{90}{y} (y(y+1)) - 5(y(y+1)) = \frac{120}{y+1} (y(y+1))$   
*LCD: (y(y+1))*  
 $90(y+1) - 5y(y+1) = 120y$   
 $90y + 90 - 5y^2 - 5y = 120y$   
 $-5y^2 + 85y + 90 = 120y$   
 $\begin{array}{r} +5y^2 - 85y - 90 \quad +5y^2 - 85y - 90 \\ \hline 0 = \frac{5y^2}{5} + \frac{35y}{5} - \frac{90}{5} \end{array}$   
 $0 = y^2 + 7y - 18$   
 $0 = (y+9)(y-2)$   
 $y + 9 = 0 \quad y - 2 = 0$   
 $\begin{array}{r} -9 \quad -9 \quad +2 \quad +2 \\ \hline y = -9 \quad y = 2 \end{array}$   
 $x = \frac{90}{-9} = -10 \quad x = \frac{90}{2} = 45$

9)  $\frac{xy}{y} = \frac{12}{y} \quad x = \frac{12}{y}$   
 $\frac{(x+1)(y-4)}{y-4} = \frac{16}{y-4}$   
 $x + 1 = \frac{16}{y-4}$   
 $\frac{12}{y} (y(y-4)) + 1(y(y-4)) = \frac{16}{y-4} (y(y-4))$   
*LCD: (y(y-4))*  
 $12(y-4) + (y(y-4)) = 16y$   
 $12y - 48 + y^2 - 4y = 16y$   
 $y^2 + 8y - 48 = 16y$   
 $\begin{array}{r} -16y \\ \hline y^2 - 8y - 48 = 0 \end{array}$   
 $(y-12)(y+4) = 0$   
 $y - 12 = 0 \quad y + 4 = 0$   
 $\begin{array}{r} +12 \quad +12 \quad -4 \quad -4 \\ \hline y = 12 \quad y = -4 \end{array}$   
 $x = \frac{12}{12} = 1 \quad x = \frac{12}{-4} = -3$   
 $(1, 12), (-3, -4)$

11)  $\frac{xy}{y} = \frac{45}{y} \quad x = \frac{45}{y}$   
 $\frac{(x-5)(y+3)}{y+3} = \frac{160}{y+3}$   
 $x - 5 = \frac{160}{y+3}$   
 $\frac{45}{y} (y(y+3)) - 5(y(y+3)) = \frac{160}{y+3} (y(y+3))$   
 $45(y+3) - 5y(y+3) = 160y$   
 $45y + 135 - 5y^2 - 15y = 160y$   
 $-5y^2 + 30y + 135 = 160y$   
 $\begin{array}{r} +5y^2 - 30y - 135 \quad +5y^2 - 30y - 135 \\ \hline 0 = \frac{5y^2}{5} + \frac{130y}{5} - \frac{135}{5} \end{array}$   
 $0 = y^2 + 26y - 27$   
 $0 = (y+27)(y-1)$   
 $y + 27 = 0 \quad y - 1 = 0$   
 $\begin{array}{r} -27 \quad -27 \quad +1 \quad +1 \\ \hline y = -27 \quad y = 1 \end{array}$   
 $x = \frac{45}{-27} = -\frac{5}{3} \quad x = \frac{45}{1}$   
 $\left(-\frac{5}{3}, -27\right), (45, 1)$